# Tail Heavy Distributions \& Confidence Levels for Directional Survey Measurements 

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## Basis of Study

- Magnetic Field study showed that declination errors are highly skewed and cant be treated as Gaussian (normal)
- Are other sources of error similar \& how does this affect confidence levels?
- To look at survey comparison data to examine the spread of differences and observe the distribution type
- 2 Survey Comparisons of the same section of hole, commonly tied
- Unit/1000 unit separation, compared Lateral and Highside Axis
- Attempt to isolate some basic sources of error
- Like Gyro/Inrun outrun comparison for drift/inclination errors
- MWD vs EMS for Sag error and Magnetic interference
- Magnetic vs Gyros from BP Alaska, Inclination Model
- Interested in 1 Dimensional confidence because most requirements are 1D

From SPE 119851 "Confidence Limits Associated with Values of the Earth's Magnetic Field used for Directional Drilling", MacMillan \& Grindrod

| TABLE 3-UNCERTAINTY ASSOCIATED WITH THE CRUSTAL FIELD, AT SIX CONFIDENCE LEVELS, CALCULATED USING DATA SETS LOCAL TO OIL AND GAS FIELDS |  |  |  |
| :---: | :---: | :---: | :---: |
| Confidence Level | Declination Limit (degrees) | Magnetic Dip Angle Limit (degrees) | Total Intensity Limit ( nT ) |
| 68.3\% (1 $\sigma$ if Gaussian) | 0.185 | 0.081 | 104 |
| 90\% | 0.403 | 0.163 | 187 |
| 95\% | 0.534 | 0.208 | 222 |
| 95.4\% (2 $\sigma$ if Gaussian) | 0.564 | 0.223 | 224 |
| 99\% | 1.191 | 0.575 | 355 |
| 99.7\% (36 if Gaussian) | 1.692 | 0.703 | 500 |

Declination Values


From SPE 36484
Towards Risk Based Well Separation Rules - Williamson


Fig. 2-Histogram showing the distribution of mean angular differences between gyroscopic and MWD surveys for 234 wells drilled in Alaska. Two theoretical distributions are shown for comparison.

## Vertical Model

1000 Vertical Wells 3D Surveyed
Displacement from Centre 13.4'/1000'



## Rate Gyros

## High Angle Gyros - Drift Inrun-Outrun Continuous Gyros 2 Types 230 comparisons

IRIOR Gyro Lateral Error


IRIOR Gyro Highside Error

- Gyro Axes
- Highside
- Along Hole




## Magnetic EMS/MWD

- EMS vs. MWD Comparisons
- 150 Examples
- Lateral = Magnetic Interference
- HighSide = Sag

EMS-MWD Lateral Error



- MWD vs EMS High Side Differences
- Mostly SAG Error

EMS-MWD Highside Error




## Conclusions

- Not many error sources are Gaussian (Normal) distributed
- Mostly have some form of heavy-tail exponential behaviour
- When sources are combined the effect is reduced (central limit theorem) - but still significant
- Confidence levels are lower than predicted with Gaussian, especially at higher sigma levels
- Can we use the same propagation mathematics but use input (1 sigma) based on $99.7 \%$ confidence and divide by 3 ?

