Education Program

Introduction to Error Modelling

Harry Wilson

ISCWSA 34, Denver, 3rd November 2011



1 © 2010 Baker Hughes Incorporated. All Rights Reserved.

Introduction to error modelling

- ISCWSA magnetic model SPE 67616
 - Read it.
- ISCWSA gyro model SPE 90408
 - Attempt to read it.



Example survey system

- Simon's carpet
- The Wilson SSE tool
 - a 3 ft steel straight edge
- How accurate?
 - We need an error model
 - Equivalent to measured depth model



Error source/ Term description			
Manufacturing tolerance			
	_	_	



Error source/ Term description			
Manufacturing tolerance			
Temp			



Error source/ Term description		
Manufacturing tolerance		
Temp		
Observation error 1		



Error source/ Term description		
Manufacturing tolerance		
Temp		
Observation error 1		
Misalignment		



Error source/ Term description		
Manufacturing tolerance		
Temp		
Observation error 1		
Misalignment		
Observation error 2 (partial)		



Error source/ Term description		
Manufacturing tolerance		
Temp		
Observation error 1		
Misalignment		
Observation error 2 (partial)		
Miscount		



Manufacturing tolerance - test data



Normal distribution (assumed)





Uncertainty – identify 1 std deviation



Error source/ Term description	Mean (ft)	1 σ (ft)	
Manufacturing tolerance	0.0	0.3	
Temp			
Observation error 1			
Misalignment			
Observation error 2 (partial)			
Miscount			



Mean

- Non-zero mean
 - Treat as bias
 - Correct for bias
 - Include bias in standard deviation
- Example, ISCWSA DST term
 - Drillstring stretch



Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	
Manufacturing tolerance	0.0	0.1	/ft	
Temp				
Observation error 1				
Misalignment				
Observation error 2 (partial)				
Miscount				



Weighting function

• More complex example:

 $-\cos\alpha \cdot [\sin/\cos^2/\sinA_m \cdot \cos\alpha \cdot (\tan\theta \cdot \cos/\theta + \sin/\cosA_m) + \sin\alpha \cdot (\tan\theta \cdot \sin/\cosA_m - \cos/\theta)]/(1 - \sin^2/\sin^2A_m)$

- Directional software
 - Each variable must be available in the database



Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station
Manufacturing tolerance	0.0	0.1	/ft	?
Temp				
Observation error 1				
Misalignment				
Observation error 2 (partial)				
Miscount				



Propagation mode station to station

- Error correlation between successive measurements
- Correlated (1) or uncorrelated (0)
 - Systematic or Random
- Straight edge?



Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station
Manufacturing tolerance	0.0	0.1	/ft	systematic
Temp				
Observation error 1				
Misalignment				
Observation error 2 (partial)				
Miscount				



Correlation coefficients - ISCWSA

ISCWSA mode	Stn - Stn	Log - Log	Well - Well
Random	0	0	0
Systematic	1	0	0
Per Well	1	1	0
Global	1	1	1



Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station
Manufacturing tolerance	0.0	0.1	/ft	systematic
Temp	Correction applied or temperature controlled (SOP)			
Observation error 1				
Misalignment				
Observation error 2 (partial)				
Miscount				



Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station	
Manufacturing tolerance	0.0	0.1	/ft	systematic	
Temp	Correction applied or temperature controlled				
Observation error 1	0.0	0.2	/ft	systematic	
Misalignment (standard app)	×				
Misalignment (buttress wall)					
Observation error 2 (partial)					
Miscount					



Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station		
Manufacturing tolerance	0.0	0.1	/ft	systematic		
Temp	Correction applied or temperature controlled					
Observation error 1	0.0	0.2	/ft	systematic		
Misalignment (standard app)	Eradicated via SOP					
Misalignment (buttress wall)						
Observation error 2 (partial)						
Miscount						



Alternative application

Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station to station		
Manufacturing tolerance	0.0	0.1	/ft	systematic		
Temp	Correction applied or temperature controlled					
Observation error 1	0.0	0.2	/ft	systematic		
Misalignment (standard app)	Eradicated via SOP					
Misalignment (buttress wall)	+0.15	0.05	/ft	random		
Observation error 2 (partial)						
Miscount						



Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station		
Manufacturing tolerance	0.0	0.1	/ft	systematic		
Temp	Correction applied or temperature controlled					
Observation error 1	0.0	0.2	/ft	systematic		
Misalignment (standard app)		Eradicated via SOP				
Misalignment (buttress wall)	+0.05	0.1	/ft & /stn	random		
Observation error 2 (partial)	0.0	0.13	/log	random		
Miscount						



Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station		
Manufacturing tolerance	0.0	0.1	/ft	systematic		
Temp	Correction applied or temperature controlled					
Observation error 1	0.0	0.2	/ft	systematic		
Misalignment (standard app)	Eradicated via SOP					
Misalignment (buttress wall)	+0.15	0.05	/ft	random		
Observation error 2 (partial)	0.0	0.13	/log	random		
Miscount	Dominant error. Must be controlled via QC test					



Directional Survey QC - Further reading

• ISCWSA - SPE 133471

- Supports 67616 and 90408



Summing errors (Standard model) Nominal survey = 61.5 ft

Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station	Contribution (1 σ, ft)
Manufacturing tolerance	0.0	0.1	/ft	systematic	6.15
Observation error 1	0.0	0.2	/ft	systematic	
Observation error 2 (partial)	0.0	0.13	/log	random	



Summing errors (Standard model) Nominal survey = 61.5 ft

Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station	Contribution (1 σ, ft)
Manufacturing tolerance	0.0	0.1	/ft	systematic	6.15
Observation error 1	0.0	0.2	/ft	systematic	12.30
Observation error 2 (partial)	0.0	0.13	/log	random	



Summing errors (Standard model) Nominal survey = 61.5 ft

(11)	(ft)	function	Propagation mode station to station	Contribution (1 σ, ft)		
0.0	0.1	/ft	systematic	6.15		
0.0	0.2	/ft	systematic	12.30		
0.0	0.13	/log	random	0.13		
Total						
	(ft) 0.0 0.0 0.0	(ft) (ft) 0.0 0.1 0.0 0.2 0.0 0.13 Total	(ft) function 0.0 0.1 /ft 0.0 0.2 /ft 0.0 0.13 /log Total	(ft)functionstation to station0.00.1/ftsystematic0.00.2/ftsystematic0.00.13/lograndomTotal		



Summing errors – correlation between terms

Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station	Contribution (1 σ, ft)
Manufacturing tolerance	0.0	0.1	/ft	systematic	6.15
Observation error 1	0.0	0.2	/ft	systematic	12.30
Observation error 2 (partial)	0.0	0.13	/log	random	0.13
	13.75				



Nominal survey = 61.5 ft (47.75 – 75.25 at 1σ)

Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station	Contribution (1 σ, ft)
Manufacturing tolerance	0.0	0.1	/ft	systematic	6.15
Observation error 1	0.0	0.2	/ft	systematic	12.30
Observation error 2 (partial)	0.0	0.13	/log	random	0.13
	13.75				



Summing errors – correlation between terms

Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station	Contribution (1 σ, ft)
Manufacturing tolerance	0.0	0.1	/ft	systematic	6.15
Observation error 1	0.0	0.2	/ft	systematic	12.30
Observation error 2 (partial)	5.19	0.13	/log	random	0.13
	13.75				



Summing errors – Alternative application

Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station	Contribution (1 σ, ft)
Manufacturing tolerance	0.0	0.1	/ft	systematic	6.15
Observation error 1	0.0	0.2	/ft	systematic	12.30
Misalignment (buttress wall)	+0.05	0.1	/ft & /stn	systematic/random	0.45
Observation error 2 (partial)	0.0	0.13	/log	random	0.13
	Total			Bias = 3.1	13.8



Nominal survey = $61.5 \text{ ft} (44.6 - 72.2 \text{ at} 1\sigma)$

Error source/ Term description	Mean (ft)	1 σ (ft)	Weighting function	Propagation mode station	Contribution (1 σ, ft)
Manufacturing tolerance	0.0	0.1	/ft	systematic	6.15
Observation error 1	0.0	0.2	/ft	systematic	12.30
Misalignment (buttress wall)	+0.05	0.1	/ft & /stn	systematic/random	0.45
Observation error 2 (partial)	0.0	0.13	/log	random	0.13
	Total			Bias = 3.1	13.8



Error model output

Bias

• Variance

- Scaleable by user to preferred confidence interval



Validation

- Is the model generally valid?
- Does a particular log conform to the model's prediction?
- Field test
- Continuous monitoring
- Reconciliation



Recap

- Error model term
 - Description
 - Mean error of distribution
 - Variance (input at 1 st dev)
 - Weighting Function
 - Correlation coefficient



Recap

- Application specific variants
 - cannot be accommodated via standard model's wfs
- Validity dependent on adherence to SOPs
 - -e.g. survey frequency
- Importance of QC tests

