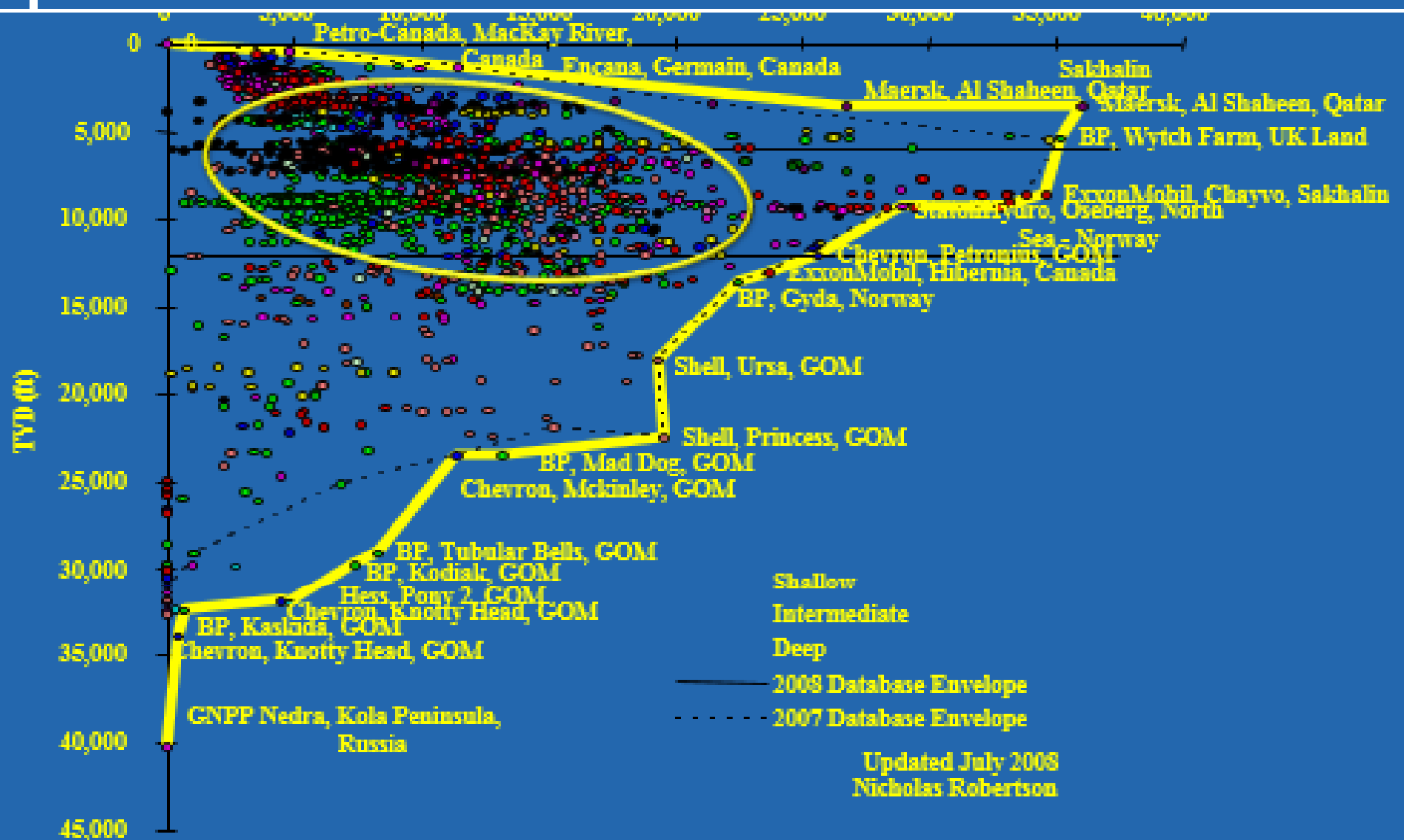


Borehole Drift – Effect of Continuous Survey on Wellbore Curvature & Torsion

Robello Samuel
Halliburton Fellow

Stretching the Space



Conventional Wellpath Designs

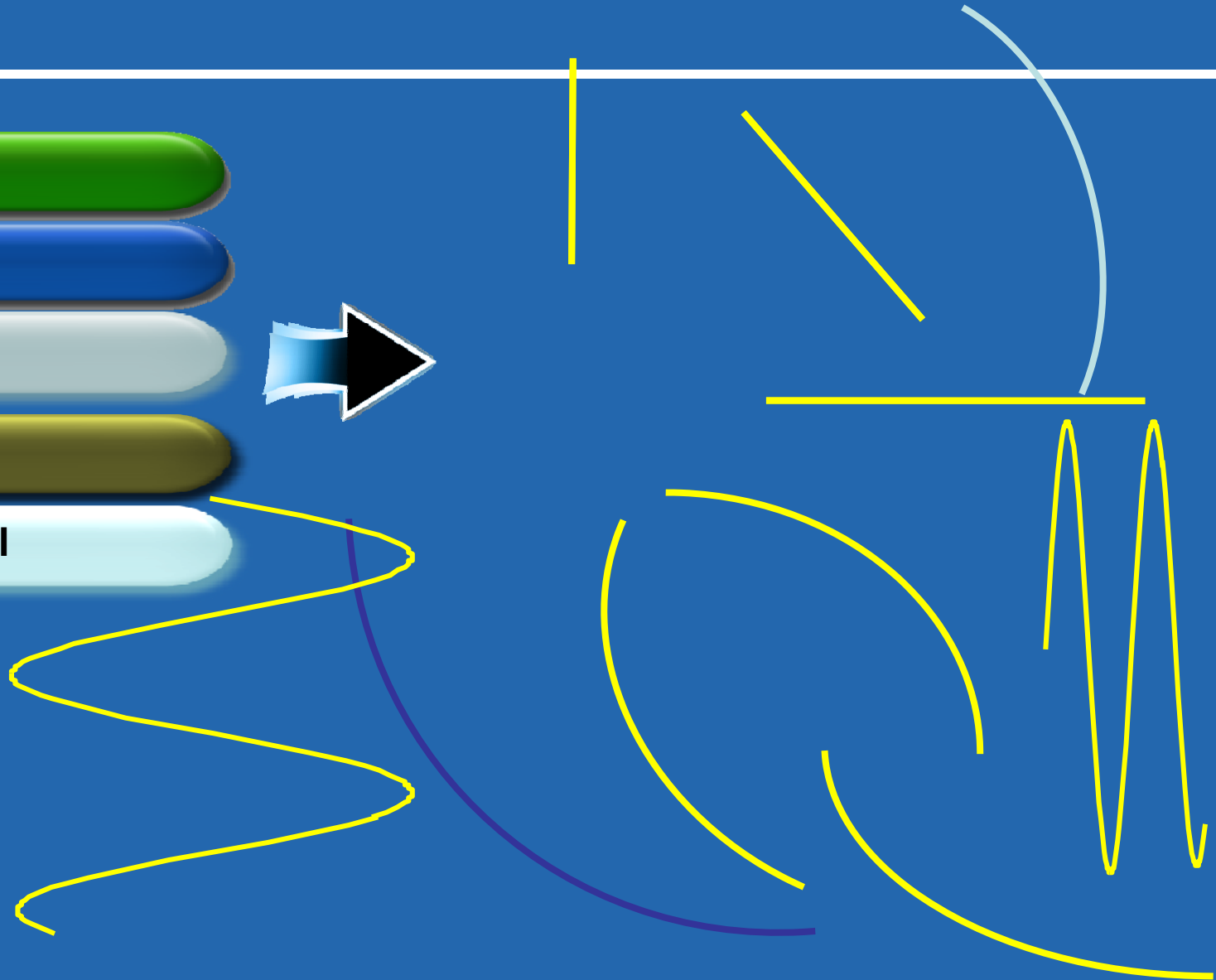
Type 1

Type 2

Type 3

Catenary

Horizontal



Are the Design Parameters Enough?

- Is the borehole shape same between all the survey intervals ?
- What is the predetermined borehole shape used ?
- What is the minimum distance of the survey interval to determine the shape?
- What are the assumptions used ?

What is the borehole shape?

Radius of Curvature Method

Minimum Curvature Method



Assume predetermined shape



Different results



Wellpath discontinuous

Design Parameters

Tortuosity

Drilling Indices

Torsion

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Wellbore Tortuosity

- **NATURAL & ARTIFICIAL TORTUOSITY**

- Sine wave method

- Helical method

- Random inclination and azimuth method

- Random inclination dependent azimuth method

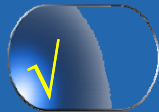
Wellbore Tortuosity



Sine Wave Tortuosity

Easy to use

$$\Delta\alpha = \sin\left(\frac{D_n}{P} \times 2\pi\right) \times M \quad \frac{2}{n} (n = 1, 2, 3..)$$



Absolute Tortuosity

Easy to quantify

$$\Gamma_{(abs)_n} = \left(\frac{\sum_{i=1}^n \alpha_{adj}}{D_n + \Delta D_n} \right)$$

Design Parameters

Tortuosity

Drilling Indices

Torsion

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1010101010111110110100001010
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Drilling Difficulty Indices

Drilling Difficulty Index

$$DDI = \log\left(\frac{D \times H \times T}{S}\right)$$

Mechanical Risk Index

Modified Mechanical Risk Index

$$TRI = \log(TDI + R_{cl} + R_{tq} + R_d + R_{bu})$$

Trajectory Risk Index

- **Qualitative Prediction**

Wellbore Score Card

- **Subjective**

Tortuosity Index

- **Weighting factors needed**

Design Parameters

Tortuosity

Drilling Indices

Torsion

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Wellbore Curvature & Torsion



• What is Wellbore Curvature

Curvature is the bend of the wellpath



• What is Wellbore Torsion

Torsion measures the departure of the wellpath from a plane, or how sharply wellpath turns

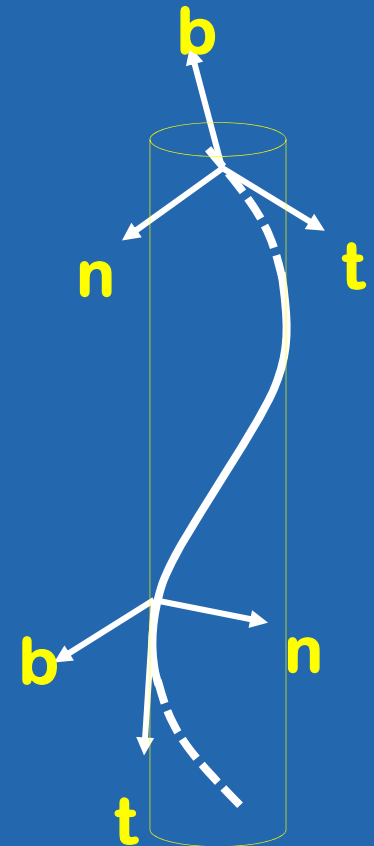
Curvature is discontinuous

- Bending Moment discontinuity

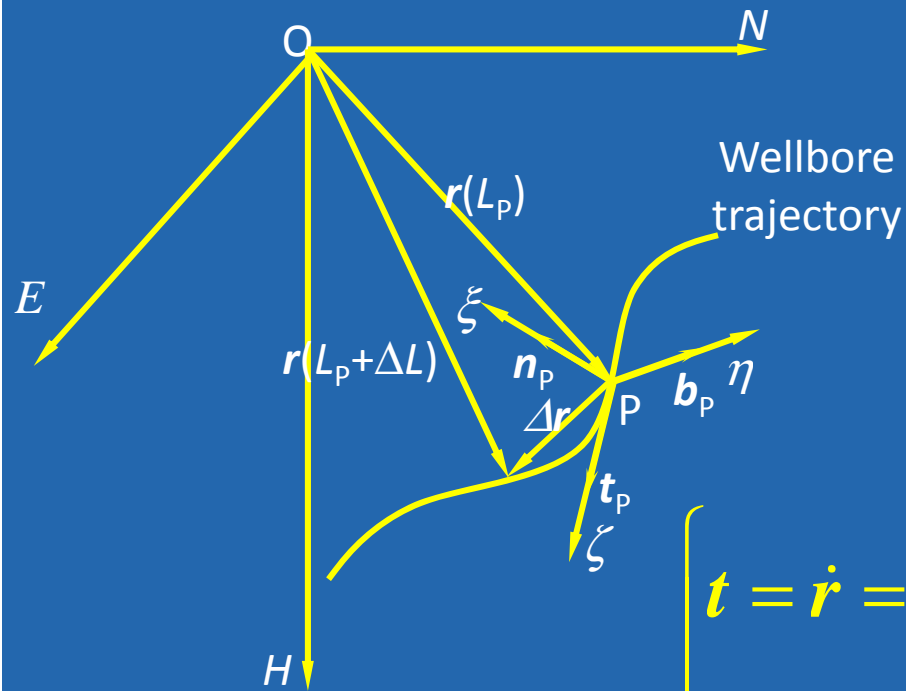
Torsion is discontinuous

- Shear Force discontinuity

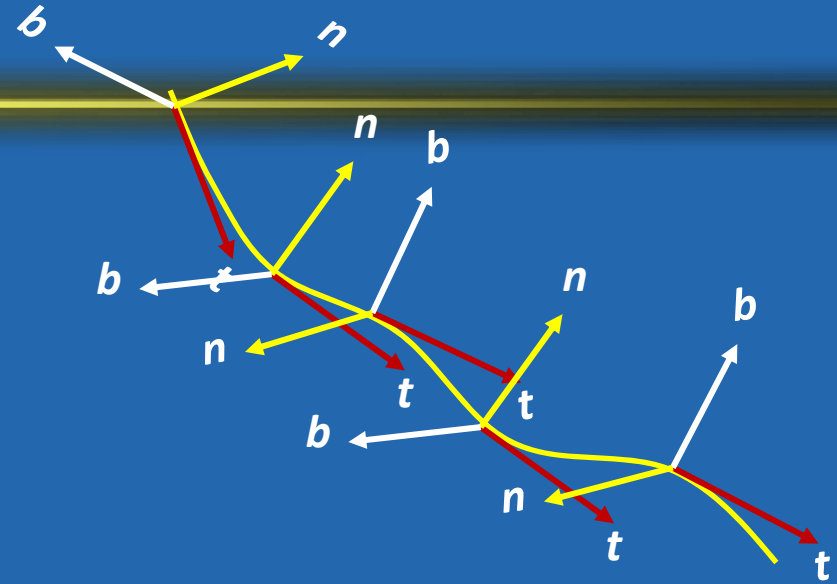
Tubular, downhole tool and SAG problems !!!



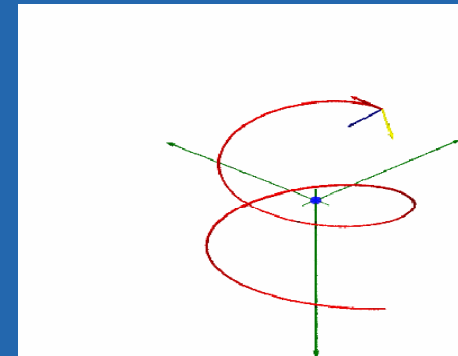
Wellbore Torsion



$$\left\{ \begin{aligned} \mathbf{t} &= \dot{\mathbf{r}} = \frac{d\mathbf{r}}{dL} \\ \mathbf{n} &= \frac{\dot{\mathbf{t}}}{|\dot{\mathbf{t}}|} = \frac{\ddot{\mathbf{r}}}{|\ddot{\mathbf{r}}|} \\ \mathbf{b} &= \mathbf{t} \times \mathbf{n} \end{aligned} \right.$$



Frenet Frame



Wellbore Torsion

Wellbore Curvature

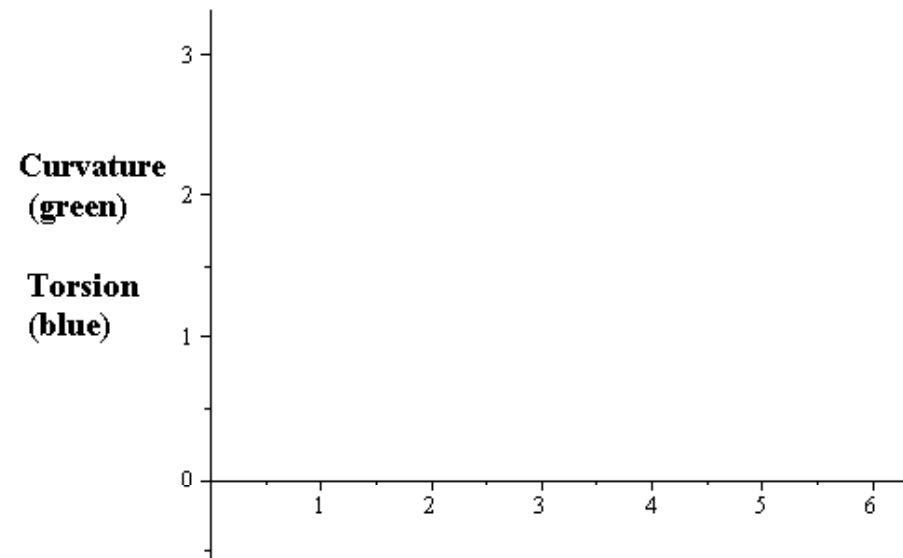
$$\kappa = \left| \frac{d\mathbf{t}}{dL} \right| = |\dot{\mathbf{t}}| \quad \Rightarrow \quad \kappa = \sqrt{\kappa_\alpha^2 + \kappa_\phi^2 \sin^2 \alpha}$$

Wellbore Torsion

$$\tau = \frac{\kappa_\alpha \dot{\kappa}_\phi - \kappa_\phi \dot{\kappa}_\alpha}{\kappa^2} \sin \alpha + \kappa_\phi \left(1 + \frac{\kappa_\alpha^2}{\kappa^2} \right) \cos \alpha$$

Effect of Wellbore Torsion on Borehole Drift

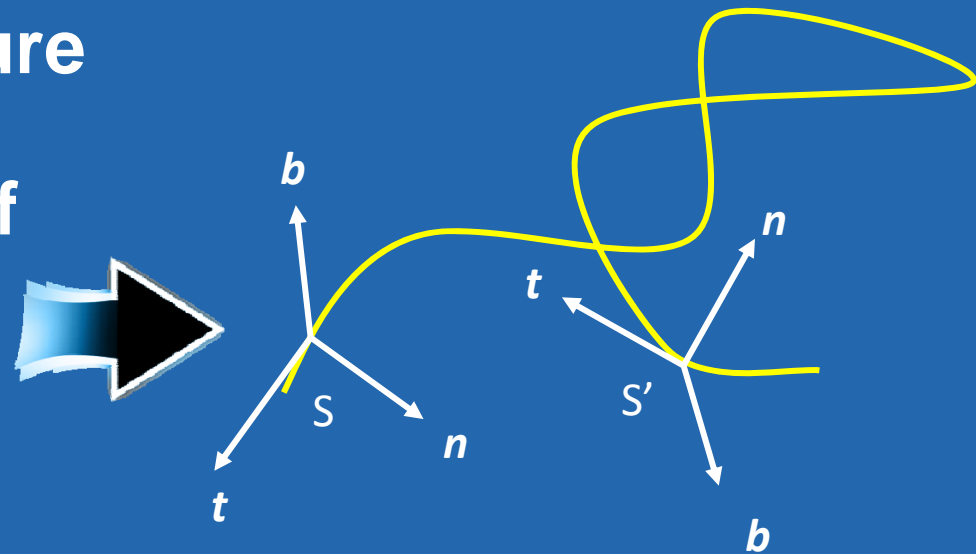
Tangent Vector – Yellow
Normal Vector – Green
Binormal Vector - Blue



Borehole shape

Functions for curvature and torsion will help to define the shape of the wellpath profile

Serret-Frenet equations fully describe a wellpath up to a Euclidean movement



Frenet/Moving

Frame

Design Parameters

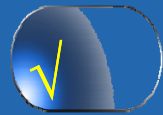
Tortuosity

Drilling Indices

Torsion

Strain Energy

Strain Energy of the Wellpath



Mathematical Technique



Physical and geometrical principles



Minimum Energy of the wellpath

Strain Energy of the Wellpath

Elastic Energy of a thin beam - it is characterized by bending and twisting least while passing through a given set of points.

Energy

$$E = \int_0^{\ell} (\kappa(x)^2 + \tau(x)^2) dx$$

Absolute Energy

$$E_{(abs)_n} = \left(\frac{\sum_{i=1}^n (\kappa_i^2 + \tau_i^2) \Delta D_i}{D_n + \Delta D_n} \right)$$

Relative Energy

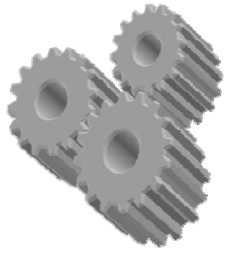
$$E_{s(rel)_n} = E_{s(abs)_n}^{cont} - E_{s(abs)_n}^{ncont}$$

Strain Energy of Special Wellpaths

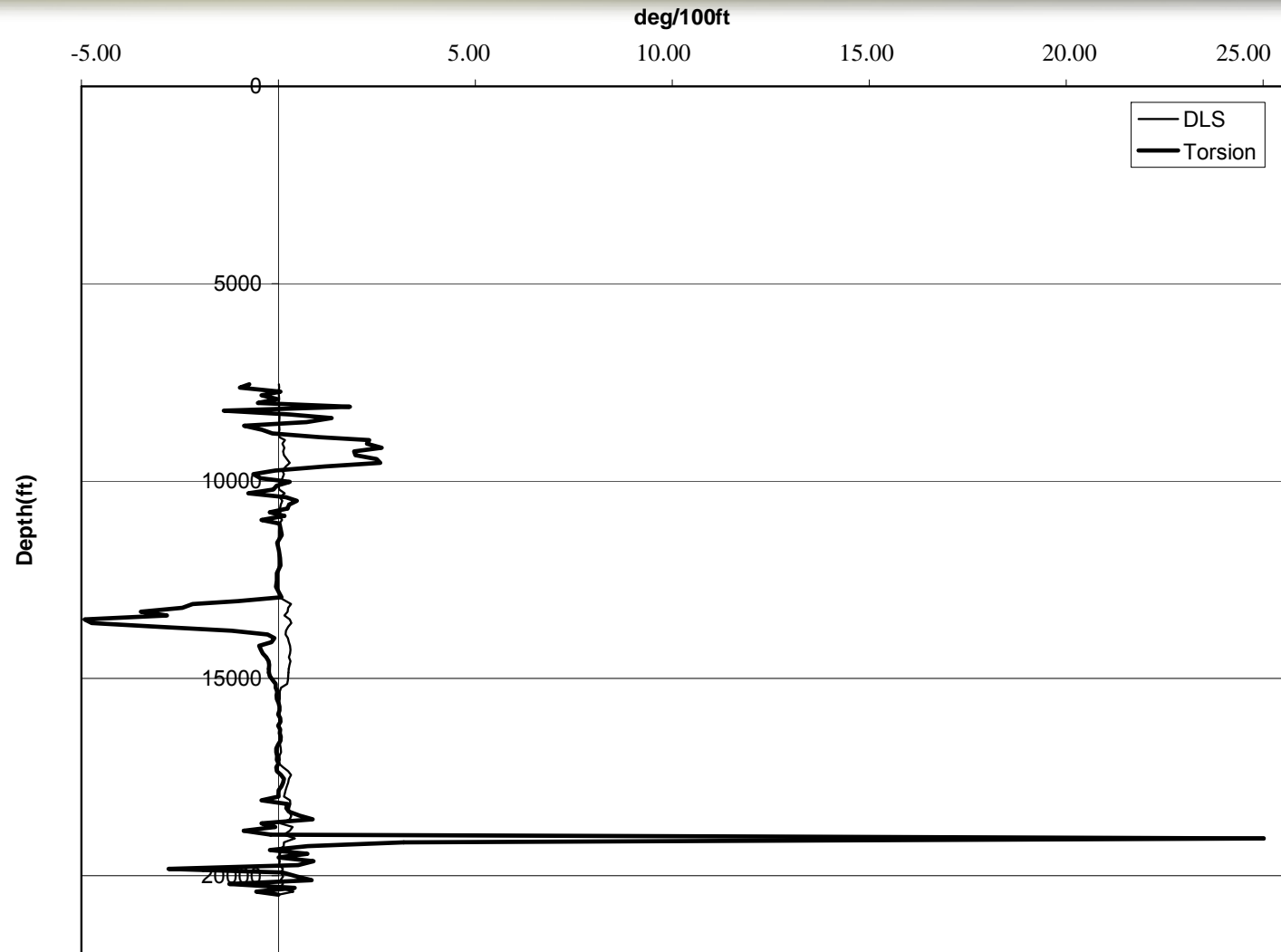
	Circular Arc	Catenary	Spiral
Curvature	$\kappa(s) = \frac{a}{\sigma^2 + b^2} u$	$\kappa(s) = \frac{180 C}{\pi a} \sin^2 \alpha$	$\kappa(s) = \frac{\pi a}{\sigma^2 + b^2} u$
Torsion	$\tau(s) = \frac{b}{\sigma^2 + b^2} u$	$\tau(s) = \kappa_\phi \left(1 - \frac{\kappa_\alpha^2}{\kappa^2} \right) \cos \alpha$	$\tau(s) = \frac{\pi b}{\sigma^2 + b^2} u$
Energy	$E = \int_0^\ell \left(\kappa(x)^2 + \tau(x)^2 \right) dx$		

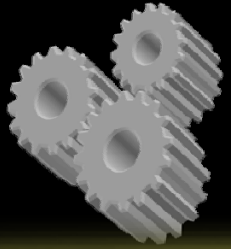
Example Studies

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Example 1



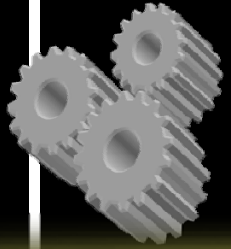


Example 2

SURVEY RESULTS WITH CALCULATED ENERGY

<u>L, ft</u>	<u>α_1</u> deg.	<u>ϕ_1</u> deg.	TVD (ft)	<u>DLS₁</u> (° /100ft)	<u>TLS₁</u> (° /100ft)	<u>Energy</u>
10000	90	360				
10090	90	360	6366.2	0	0	0

<u>L, ft</u>	<u>α_1</u> deg.	<u>ϕ_1</u> deg.	TVD (ft)	<u>DLS₁</u> (° /100ft)	<u>TLS₁</u> (° /100ft)	<u>Energy</u>
10000	90	360				
10045	92	358		9.4	2.3	.1824
10090	90	360	6363.1	9.4	.00002	.1666

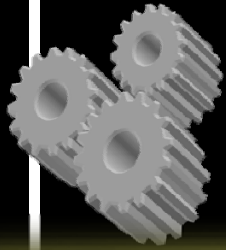


Example 2

SURVEY RESULTS WITH CALCULATED ENERGY

<u>L, ft</u>	<u>α_1</u> deg.	<u>ϕ_1</u> deg.	TVD (ft)	<u>DLS,</u> (° /100ft)	<u>TLS,</u> (° /100ft)	<u>Energy</u>
10000	90	360				
10090	90	360	6366.2	0	0	0

<u>L, ft</u>	<u>α_1</u> deg.	<u>ϕ_1</u> deg.	TVD (ft)	<u>DLS,</u> (° /100ft)	<u>TLS,</u> (° /100ft)	<u>Energy</u>
10000	90	360				
10015	92	359		14.90	8.5	.4418
10045	90	358		7.45	2.3	.1824
10060	94	359		14.90	-8.5	.4417
10090	90	360	6363.1	7.45	00002	.1666



Example 2

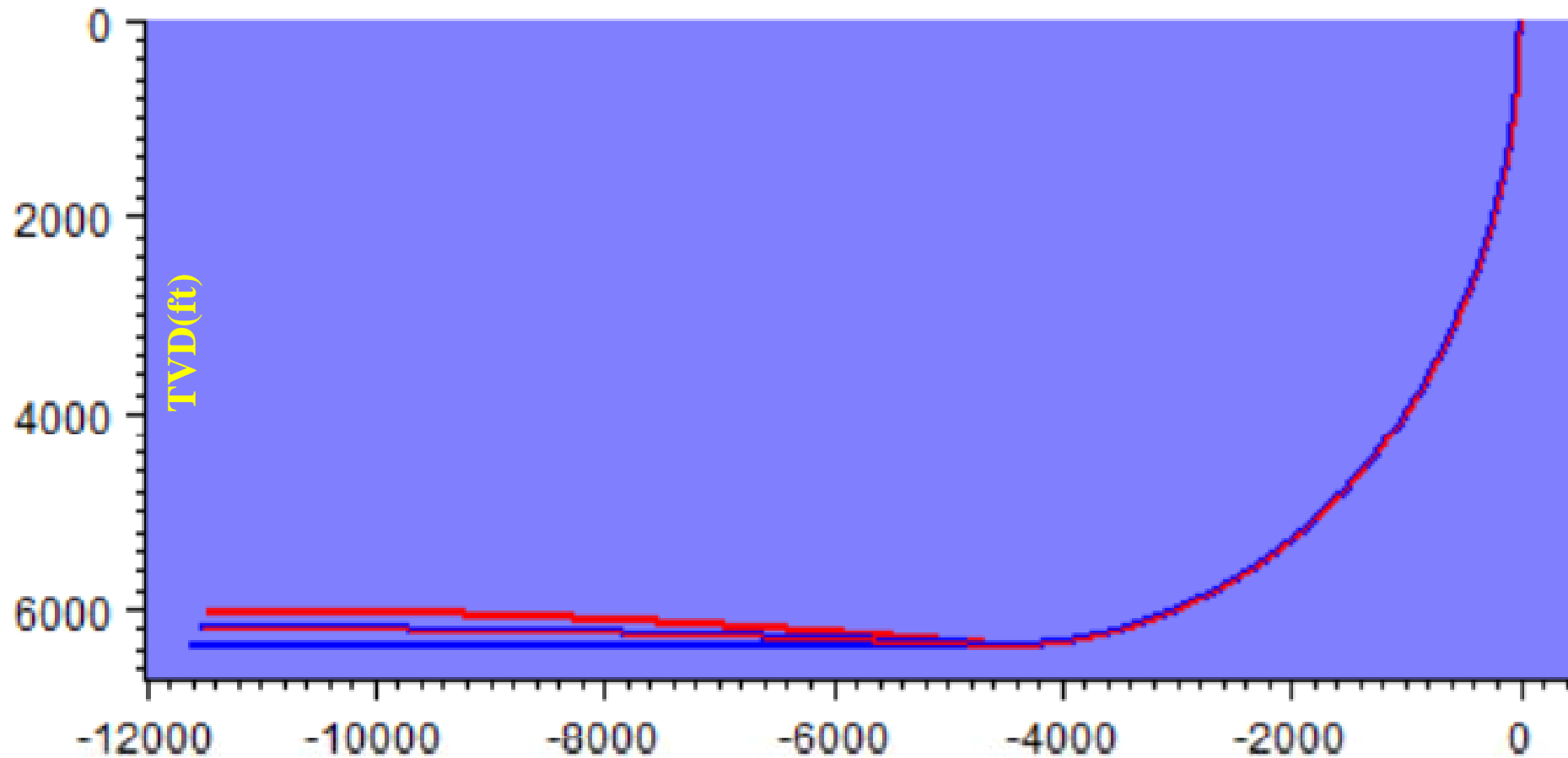
SURVEY RESULTS WITH CALCULATED ENERGY

<u>L, ft</u>	<u>α_1</u> deg.	<u>ϕ_1</u> deg.	TVD (ft)	<u>DLS₁</u> (° /100ft)	<u>TLS₁</u> (° /100ft)	<u>Energy</u>
10000	90	360				
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10000	90	360				
10015	92	359		14.90	8.5	.4418
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10060	94	359		14.90	-8.5	.4417
10090	92	360	6363.1	7.45	00002	.1666

Cascading Effects

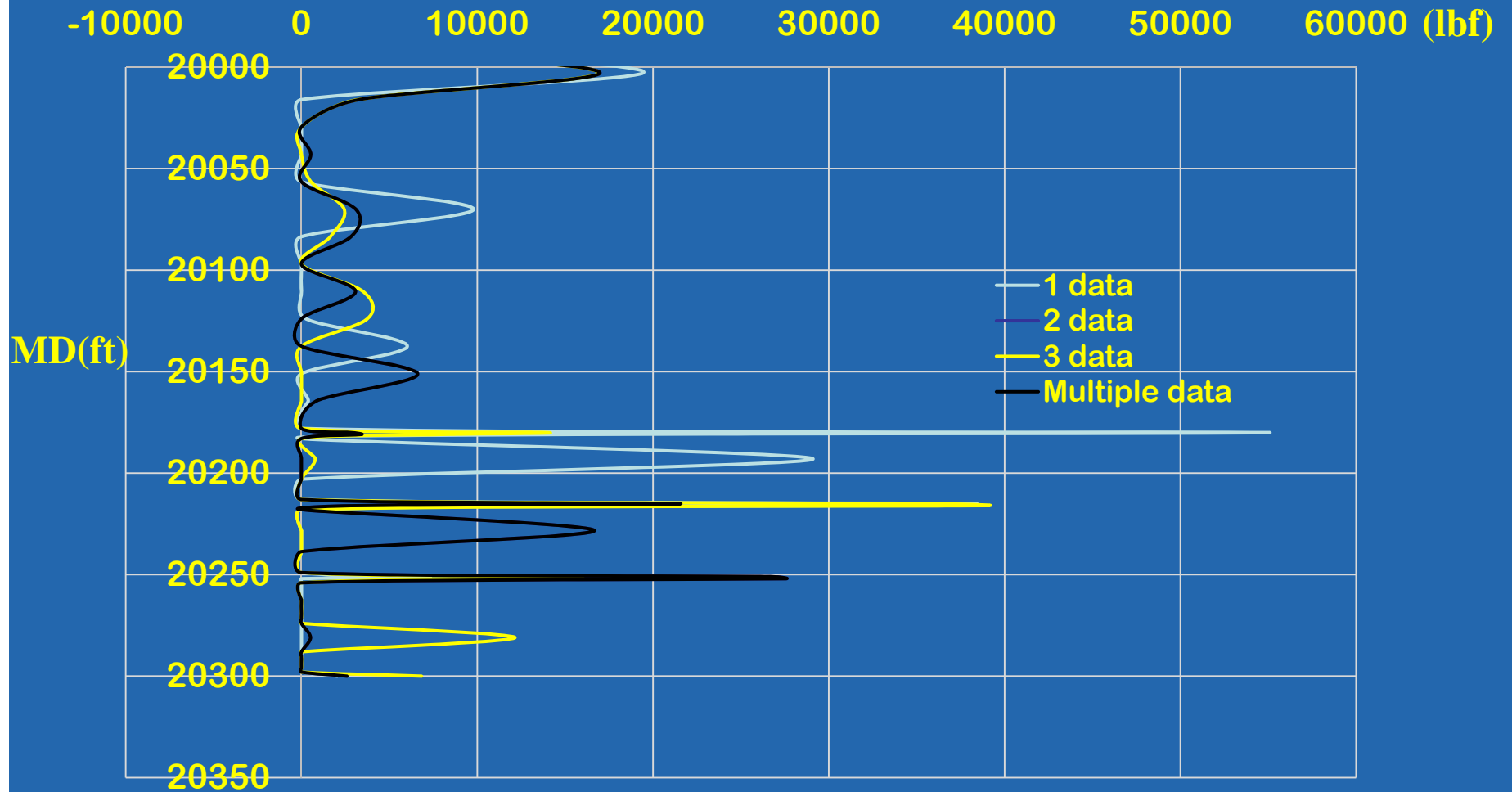
- Estimation of side force
- Estimation of drag
- Estimation of torque
- Estimation of hook load
- Estimation of friction factor
- Estimation of SAG

Vertical Section

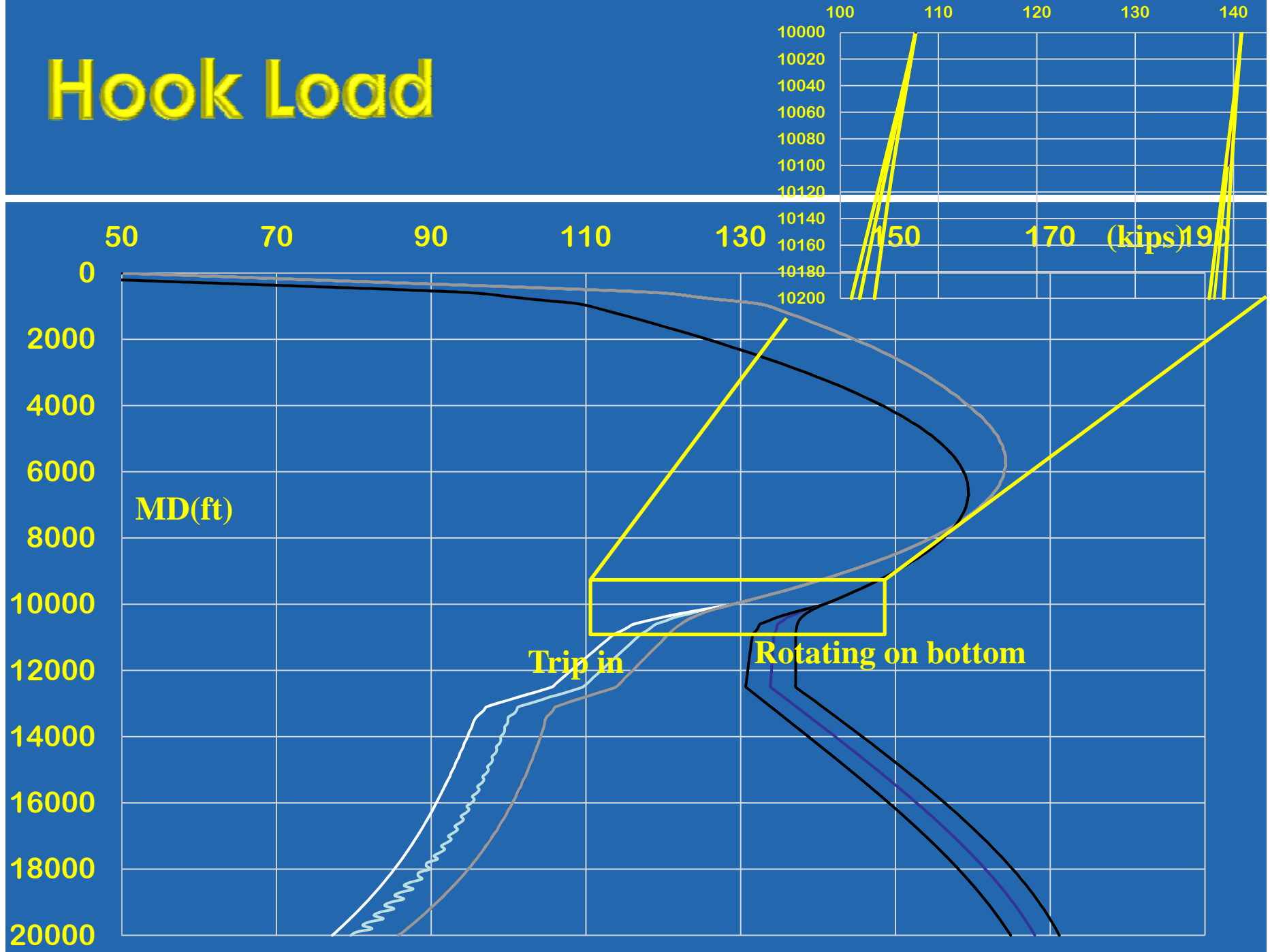


Vertical Section (ft)

Effect of Side Force

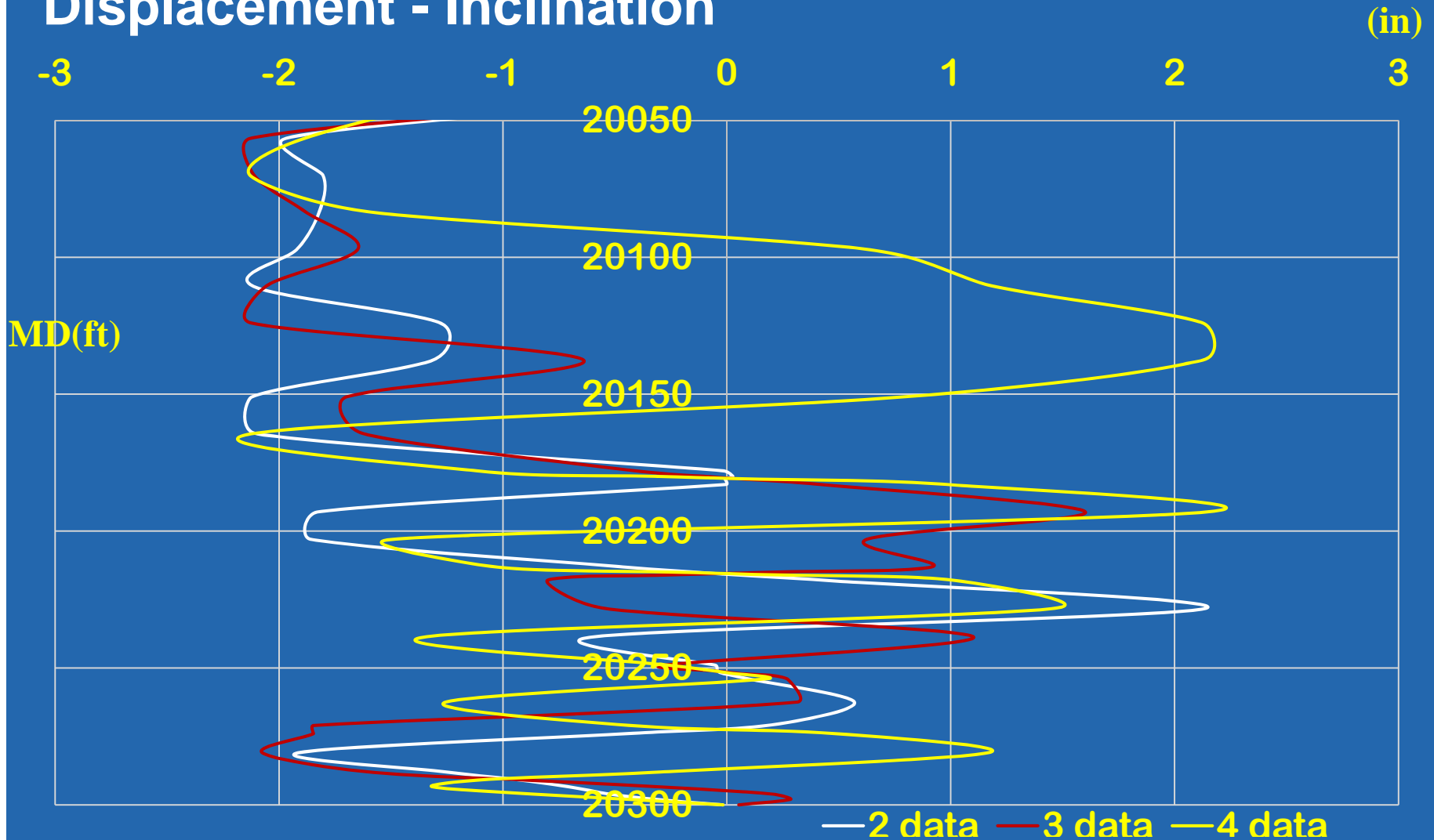


Hook Load



Effect of SAG

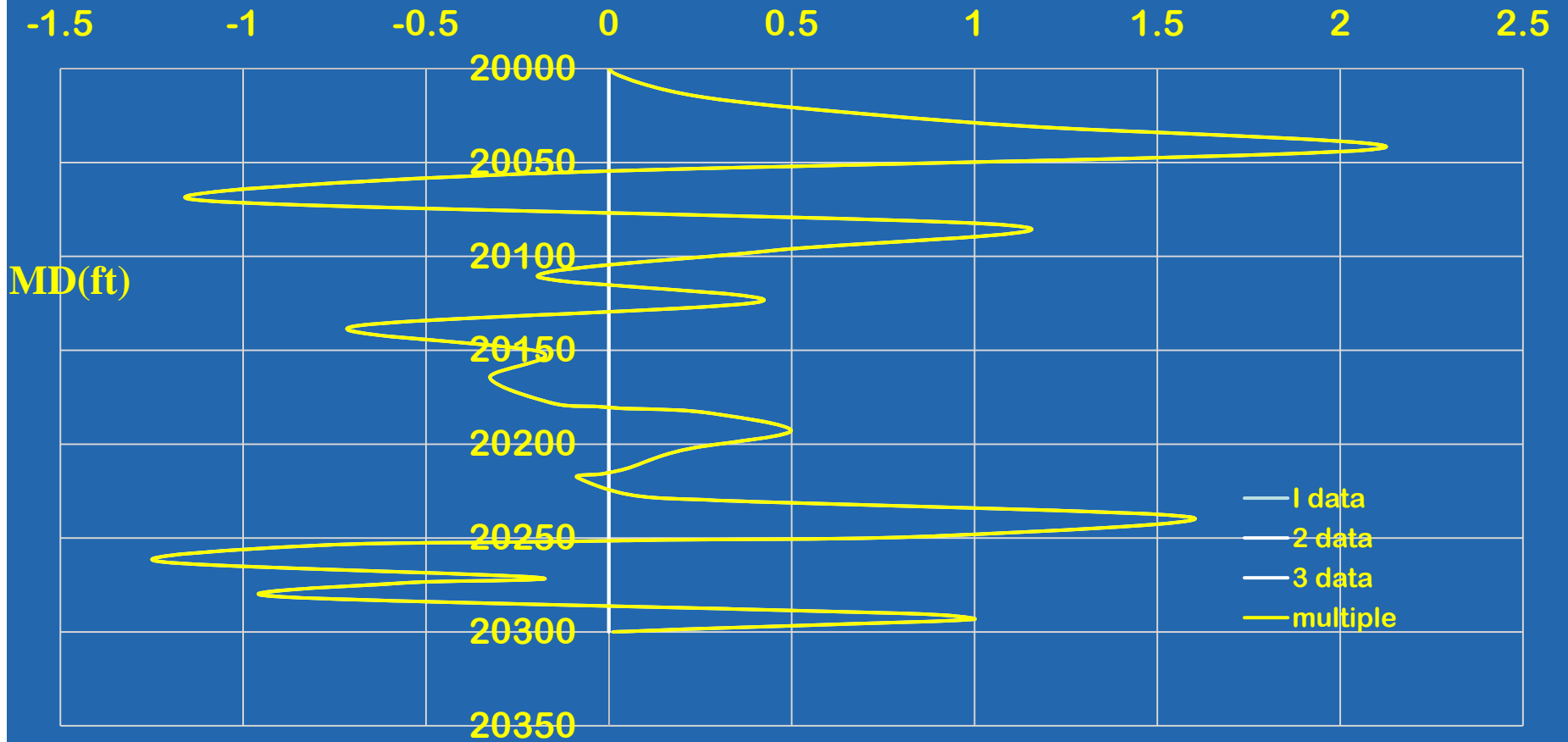
Displacement - Inclination







Effect of SAG

Displacement - Direction

(in)



Conclusions

-  Wellbore curvature and torsion at survey stations well define the shape of a wellbore within a survey interval.
-  3D energy based criterion provides a method to compare the wellpath profiles with different survey intervals
-  The results are more precise when the wellbore curvature and torsion are synchronously involved over every course length.
-  Mechanical calculations will be skewed

Q & A

Robello Samuel
Halliburton Fellow

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